## Model Question Paper

## Undergraduate Programme - Mathematics

SHADE the correct Response viz., A, B, C, D or E in the RESPONSE SHEET. Each Question carry ONE mark.

## SAMPLE QUESTIONS

Question 1: Which one of the following statements is FALSE?
(A) In the expansion of $(a+b)^{n}$, the $r^{\text {th }}$ term is $\binom{n}{r} a^{n-r} b^{r}$
(B) If A and B are square matrices, then $\operatorname{det}(A B)=\operatorname{det}(A) \cdot \operatorname{det}(B)$
(C) In a geometric series, the ratio of any two successive terms is constant
(D) The equation $x^{4}+x^{2}+1$ has two real quadratic factors
(E) The inverse of $a+b i$ is $\frac{a}{a^{2}+b^{2}}+\frac{-b}{a^{2}+b^{2}} i$

Question 2: What are the roots of the equation $12 x^{3}+16 x^{2}-3 x=0$ ?
(A) 0 only
(B) $-3 / 2$ and $1 / 6$ only
(C) $3 / 2$ and $-1 / 6$ only
(D) $0,3 / 2$ and $-1 / 6$
(E) $0,-3 / 2$ and $1 / 6$

Question 3: Which one of the following is TRUE ?
(A) $\sin 150^{\circ}=-\sin 30^{\circ}$
(B) $\sin 30^{\circ}=\frac{2 \tan 15^{\circ}}{1+\tan ^{2} 15^{\circ}}$
(C) $\sin 15 i=i \cosh 15$
(D) $a^{2}=b^{2}+c^{2}-2 b c \sin A$
(E) $\cos 75^{\circ}=\sin 45^{\circ} \cos 30^{\circ}-\sin 30^{\circ} \cos 45^{\circ}$

Question 4: What are the values of $x$ in $[0,2 \pi]$ that satisfy the trigonometric equation $\sin x+\cos x=0$ ?
(A) $5 \pi / 4$ and $7 \pi / 4$
(B) $3 \pi / 4$ and $5 \pi / 4$
(C) $3 \pi / 4$ and $7 \pi / 4$
(D) $\pi / 4$ and $3 \pi / 4$
(E) $\pi / 4$ and $5 \pi / 4$

Question 5: Which one of the following expressions is meaningful?
(A) $\vec{a} \cdot \vec{b} \cdot \vec{c}$
(B) $\vec{a} \times \vec{b} \times \vec{c}$
(C) $\vec{a} \vec{b} \cdot c$
(D) $a \vec{b} \times \vec{c}$
(E) $\vec{a} \cdot b \times \vec{c}$

Question 6: Which one of the following is FALSE?
(A) $\vec{a}+\vec{b}=\vec{b}+\vec{a}$
(B) $\vec{a} \cdot \vec{b}=\vec{b} \cdot \vec{a}$
(C) $\vec{a} \times \vec{b}=\vec{b} \times \vec{a}$
(D) $\vec{a}+\overrightarrow{0}=\vec{a}$
(E) $\vec{a} \times \overrightarrow{0}=\overrightarrow{0}$

Question 7: Given the marks - $20,10,0,12,13,10,5,10,0,20$ - obtained by students in a test for 20 marks, which one of the following is FALSE ?
(A) mean marks is 10
(B) median marks is 10
(C) modal marks is 10
(D) range of marks is 10
(E) total number of observations is 10

Question 8: Two unbiased dice are thrown. What is the probability that the sum of numbers on the dice is 7 ?
(A) $7 / 36$
(B) $1 / 6$
(C) $5 / 36$
(D) $2 / 9$
(E) $1 / 12$

Question 9: How many 3-digit odd numbers can be formed using the digits $0,1,2,3,6,9$ ?
(A) 60
(B) 90
(C) 216
(D) 75
(E) 180

Question 10: What is the slope and the $x$ - intercept of the straight line $2 x+3 y-4=0$, respectively?
(A) $-2 / 3$ and $4 / 3$
(B) $2 / 3$ and 2
(C) $2 / 3$ and $-4 / 3$
(D) $-2 / 3$ and 2
(E) $-2 / 3$ and $4 / 3$

Question 11: What is the equation of the ellipse with one focus at $\left(\frac{1}{\sqrt{2}}, 0\right)$ and one vertex at $(0,-1)$ ?
(A) $2 x^{2}+3 y^{2}=3$
(B) $x^{2}+3 y^{2}=3$
(C) $2 x^{2}+3 y^{2}=1$
(D) $2 x^{2}+3 y^{2}=6$
(E) $2 x^{2}+y^{2}=3$

Question 12: Classify $f: \mathbb{R} \rightarrow \mathbb{R}$ be defined by $f(x)=x^{2}$.
(A) not a function
(B) both one-to-one and onto
(C) one-to-one but not onto
(D) not one-to-one but onto
(E) neither one-to-one and onto

Question 13: What is the derivative of $2 x^{3}+6 x^{2}+5$ with respect to $x^{2}+4 x-1$ ?
(A) $3 x$
(B) $6 x^{2}+12 x$
(C) $2 x$
(D) $2 x+4$
(E) $3 x+1$

Question 14: If $\int x \cdot u(x) d x=\log \log x$, then what is $u(x)$ :
(A) $\frac{1}{x \log x}$
(B) $\frac{1}{x^{2} \log x}$
(C) $\frac{1}{x}$
(D) $\frac{1}{x^{2}}$
(E) $\log x$

Question 15: Let $f: R \rightarrow R$ be defined by $f(x)=\sqrt{x^{2}-4}$, then the largest domain in which $f$ is continuous is $\qquad$
(A) $R$
(B) $[2, \infty)$
(C) $(-\infty,-2]$
(D) $(-\infty,-2] \cup[2, \infty)$
(E) $[-2,2]$

